

Exercise 1 : (justify each answer)

1- Let  $A = 76_{(10)}$  and  $B = -83_{(10)}$ .

*(  $A = 91_{(10)}$  and  $B = -72_{(10)}$  ) (  $A = 76_{(10)}$  and  $B = -83_{(10)}$  )*

a. Represent A and B in C2 on 8 bits

$$A=62_{(10)} = 0011\ 1110_{(c2)}$$

$$109 = 0110\ 1101_{(c2)}$$

$$B=-109_{(10)} = 1001\ 0011_{(c2)}$$

$$A=91_{(10)} = 0101\ 1011_{(c2)}$$

$$72 = 0100\ 1000_{(c2)}$$

$$B=-72_{(10)} = 1011\ 1000_{(c2)}$$

$$A=76_{(10)} = 0100\ 1100_{(c2)}$$

$$83 = 0101\ 0011_{(c2)}$$

$$B=-83_{(10)} = 1010\ 1101_{(c2)}$$

b. Compute  $(-A - B)$  in C2 on 8 bits. Indicate the overflow, carry, and check the result in decimal.

$$-A - B = c2(62) + 109 = C2(0011\ 110) + 0110\ 1101 = 0010\ 1111_{(c2)} \text{ overflow no, carry yes}$$

$$-A - B = c2(91) + 72 = C2(0101\ 1011) + 0100\ 1000 = 1110\ 1101_{(c2)} \text{ overflow no, carry no}$$

$$-A - B = c2(76) + 83 = C2(0100\ 1100) + 0101\ 0011 = 0000\ 0111_{(c2)} \text{ overflow no, carry yes}$$

2- Let  $A = 100100_{(c2)}$  and  $B = (10010100)_{(sm/sva)}$ .

*(  $A = 101100_{(c2)}$  and  $B = (10001100)_{(sm/sva)}$  ) and (  $A = 110100_{(c2)}$  and  $B = (10011100)_{(sm/sva)}$  )*

Compute  $(A+B)$  in C2 on 8bits. Indicate the overflow, carry, and check the result in decimal.

$$A = 11100100_{(c2)} = -28_{(10)}$$

$$B = 10010100_{(sm/sva)} = -0010100_{(2)} = -20 = c2(00010100) = 11101100_{(c2)}$$

$$A+B = 11100100+11101100 = 11010000_{(c2)} = -48_{(10)} \text{ overflow no, carry yes}$$

$$A = 11101100_{(c2)} = -20_{(10)}$$

$$B = 10001100_{(sm/sva)} = -0001100_{(2)} = -12 = c2(00001100) = 11110100_{(c2)}$$

$$A+B = 11101100+11110100 = 11100000_{(c2)} = -32_{(10)} \text{ overflow no, carry yes}$$

$$A = 11110100_{(c2)} = -12_{(10)}$$

$$B = 10011100_{(sm/sva)} = -0011100_{(2)} = -28 = c2(00011100) = 11100100_{(c2)}$$

$$A+B = 11110100+11100100 = 11011000_{(c2)} = -40_{(10)} \text{ overflow no, carry yes}$$

3- Let  $A = -110.0110_{(2)}$  and  $B = 0010\ 0110.0110\ 0010\ 0101_{(BCD)}$ .

*(  $A = -100.0110_{(2)}$  and  $B = 0010\ 0011.0110\ 0010\ 0101_{(BCD)}$  ) (  $A = -101.0110_{(2)}$  and  $B = 0010\ 1001.0110\ 0010\ 0101_{(BCD)}$  )*

Represent A and B in the IEEE 754 standard.

$$A = -110.0110 = -1.100110 * 2^2 \quad s=- \quad m = 0.100110 \quad e = 2 \quad c = 2+127 = 129 = 10000001_{(2)}...$$

$$A = 1\ 10000001\ 100110000000000000000000$$

$$B = 26.625 = 00011010.101 = 1.1010101 * 2^4 \quad s=+ \quad m = 0.1010101 \quad e = 4 \quad c = 4+127 = 131 = 10000011$$

$$B = 0\ 10000011\ 101010100000000000000000$$

$$A = -100.0110 = -1.000110 * 2^2 \quad s=- \quad m = 0.000110 \quad e = 2 \quad c = 2+127 = 129 = 10000001_{(2)}...$$

$$A = 1\ 10000001\ 000110000000000000000000$$

$$B = 23.625 = 00010111.101 = 1.0111101 * 2^4 \quad s=+ \quad m = 0.0111101 \quad e = 4 \quad c = 4+127 = 131 = 10000011$$

$$B = 0\ 10000011\ 011110100000000000000000$$

$$A = -101.0110 = -1.010110 * 2^2 \quad s=- \quad m = 0.010110 \quad e = 2 \quad c = 2+127 = 129 = 10000001_{(2)}...$$

$$A = 1\ 10000001\ 010110000000000000000000$$

$$B = 29.625 = 00011101.101 = 1.1101101 * 2^4 \quad s=+ \quad m = 0.1101101 \quad e = 4 \quad c = 4+127 = 131 = 10000011$$

$$B = 0\ 10000011\ 110110100000000000000000$$

a. Compute (A + B) in the IEEE 754 standard.

$$A+B = -1.10011 \cdot 2^2 + 110.10101 \cdot 2^2 = 101.0001 \cdot 2^2 = 1.010001 \cdot 2^4$$

$$S = + \quad m = 0.010001 \quad e = 4 \quad c = 131 = 10000011$$

$$A+B = 0 \quad 10000011 \quad 010001000000000000000000$$

$$A+B = -1.000110 \cdot 2^2 + 101.11101 \cdot 2^2 = 100.11101 \cdot 2^2 = 1.0011101 \cdot 2^4$$

$$S = + \quad m = 0.0011101 \quad e = 4 \quad c = 131 = 10000011$$

$$A+B = 0 \quad 10000011 \quad 001110100000000000000000$$

$$A+B = -1.010110 \cdot 2^2 - 111.01101 \cdot 2^2 = 110.0001 \cdot 2^2 = 1.100001 \cdot 2^4$$

$$S = + \quad m = 0.100001 \quad e = 4 \quad c = 131 = 10000011$$

$$A+B = 0 \quad 10000011 \quad 100001000000000000000000$$

4- Let  $A = 1001 \ 0101_{(BCD)}$ ,  $B = 10100010_{(Gray)}$ .  $C = B+2$

$(A = 1001 \ 0111_{(BCD)}, B = 11000101_{(Gray)}) (A = 1001 \ 0000_{(BCD)}, B = 10100101_{(Gray)})$

a. Give the value of C without conversion to base 2.

b. Compute (A + B) in BCD.

a)  $B = 10100010_{(gray)}$

→  $B+1 = 10100110_{(gray)}$  (number of 1 is odd)

→  $C=B+2 = 10100111_{(gray)}$  (number of 1 is even)

b)  $A=1001 \ 0101_{(BCD)} = 95_{(10)}$        $B = 11110011_{(2)} = 143_{(10)} = 0001 \ 0100 \ 0011_{(bcd)}$

$A+B = 0010 \ 0011 \ 1000_{(bcd)} = 238_{(10)}$

a)  $B = 11000101_{(gray)}$

→  $B+1 = 11000100_{(gray)}$  (number of 1 is even)

→  $C=B+2 = 11001100_{(gray)}$  (number of 1 is odd)

b)  $A=1001 \ 0111_{(BCD)} = 97_{(10)}$        $B = 10100111_{(2)} = 167_{(10)} = 0001 \ 0110 \ 0111_{(bcd)}$

$A+B = 0010 \ 0110 \ 0100_{(bcd)} = 264_{(10)}$

a)  $B = 10100101_{(gray)}$

→  $B+1 = 10100100_{(gray)}$  (number of 1 is odd)

→  $C=B+2 = 10101100_{(gray)}$  (number of 1 is even)

b)  $A=1001 \ 0000_{(BCD)} = 90_{(10)}$        $B = 11110111_{(2)} = 198_{(10)} = 0001 \ 1001 \ 1000_{(bcd)}$

$A+B = 0011 \ 0011 \ 0111_{(bcd)} = 288_{(10)}$

a)  $B = 10100101_{(gray)}$

→  $B+1 = 10100100_{(gray)}$  (number of 1 is odd)

→  $C=B+2 = 10101100_{(gray)}$  (number of 1 is even)

b)  $A=1001 \ 1000_{(BCD)} = 90_{(10)}$        $B = 11110111_{(2)} = 198_{(10)} = 0001 \ 1001 \ 1000_{(bcd)}$

$A+B = 0011 \ 0011 \ 0111_{(bcd)} = 288_{(10)}$

5- Sachant que ' $A' = 41_{(16)}$ , ' $a' = 61_{(16)}$ ', ' $O' = 30_{(16)}$  et espace =  $20_{(16)}$ .

Donner la codification en ASCII de **votre** date de naissance exemple : « 01 Janvier 2000 ».